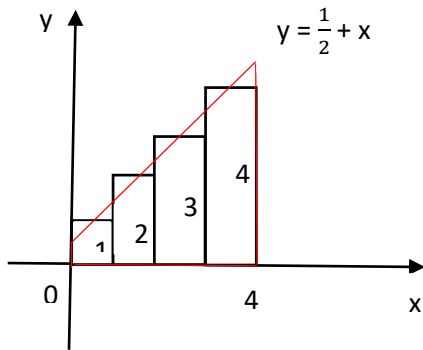


Integration

Given a line ,

$y = \frac{1}{2} + x$; Find the area from 0 to 4



$$\int_0^4 \left(\frac{1}{2} + x\right) dx = ?$$

$$\begin{aligned} \int_0^4 \left(\frac{1}{2} + x\right) dx &= \left[\frac{1}{2}x + \frac{x^2}{2}\right]_0^4 = \\ &= \frac{1}{2} \cdot 4 + \frac{4^2}{2} - (0+0) = 2+8-0 = 10 \end{aligned}$$

$$\int_0^{10} \left(\frac{1}{2} + x\right) dx = \left[\frac{1}{2}x + \frac{x^2}{2}\right]_0^{10} = \frac{1}{2} \cdot 10 + \frac{10^2}{2} = 5+50 = 55$$

The sum of rectangular is

$$1+2+3+4+5+6+7+8+9+10 = \frac{10}{2}(1+10) = 55$$