

Find the parameters parabola

Given: $y'(1) = 3$, the slope

$B(1,6)$

$x = \frac{1}{4}$, Min

$$y = ax^2 + bx + c$$

$$y' = 2ax + b$$

$$y'(1) = 2a \cdot 1 + b = 3$$

$$y' = 2ax + b$$

$$y'\left(\frac{1}{4}\right) = 0 \quad \Rightarrow \quad 2a \cdot \frac{1}{4} + b = 0$$

$$\frac{a}{2} + b = 0$$

$$2a + b = 3$$

$$\frac{a}{2} + b = 0$$

$$1\frac{1}{2}a = 3 \quad a = 2$$

$$b = -1$$

$$B(1,6) \Rightarrow 6 = a + b + c$$

$$6 = 2 + (-1) + c$$

$$c + 1 = 6$$

$$c = 5$$

The Parabola is

$$y = 2x^2 - x + 5$$