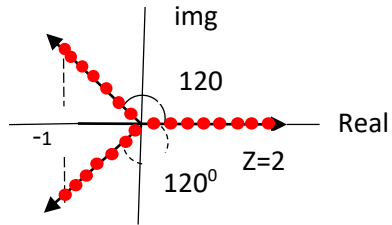


Complex Number $z^3 = 8$

$$z^3 = 8$$



$$\frac{360^\circ}{3} = 120^\circ$$

$$|Z| = 2$$

$$\cos 0^\circ + i \sin 0^\circ = 1$$

$$Z_1 = 2(\cos 0^\circ + i \sin 0^\circ) = 2$$

$$Z_2 = 2(\cos 120^\circ + i \sin 120^\circ) = -1 + \sqrt{3}i$$

$$Z_3 = 2(\cos 240^\circ + i \sin 240^\circ) = -1 - \sqrt{3}i$$

$$x^4 + \frac{1}{2}x^3 - 8x - 4 = 0$$

$x = 2$ is a solution

$$2^4 + \frac{1}{2}2^3 - 8 \cdot 2 - 4 = 0$$

$$16 + 4 - 16 - 4 = 0$$

$$x^3(x + \frac{1}{2}) - 4(2x + 1) = 0$$

$$x^3(x + \frac{1}{2}) - 4 \cdot 2(x + \frac{1}{2}) = 0$$

$$(x^3 - 8)(x + \frac{1}{2}) = 0$$

\swarrow $x^3 = 8$ \searrow $x = -\frac{1}{2}$

(1) $x = 2$

(2) $x = -1 + \sqrt{3}i$

(3) $x = -1 - \sqrt{3}i$

$$x_1 + x_2 + x_3 = 0$$