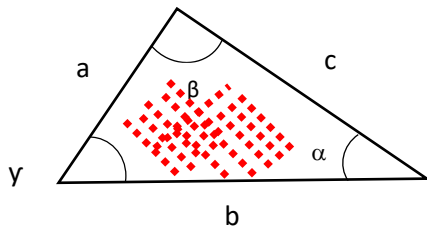


$$\text{Trigo} \Rightarrow \frac{a}{\sin \alpha} = 2R$$



$$\text{Prove} \Rightarrow \frac{\sin(\alpha - \beta)}{\sin(\alpha + \beta)} = \frac{a^2 - b^2}{c^2}$$

$$\begin{aligned} \sin(\alpha + \beta) &= \sin(180 - \gamma) \\ &= \sin \gamma \end{aligned}$$

$$\frac{a}{\sin \alpha} = 2R \Rightarrow a = 2R \sin \alpha$$

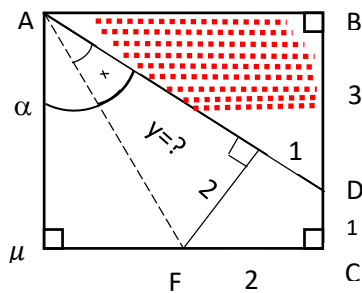
$$b = 2R \sin \beta$$

$$a^2 - b^2 = 4R^2(\sin^2 \alpha - \sin^2 \beta)$$

$$\frac{a^2 - b^2}{c^2} = \frac{4R^2(\sin^2 \alpha - \sin^2 \beta)}{4R^2 \sin^2 \gamma} =$$

$$= \frac{2\sin^2 \alpha - 2\sin^2 \beta}{2\sin^2 \gamma} = \frac{(1 - \cos 2\alpha) - (1 - \cos 2\beta)}{2\sin^2 \gamma} = \frac{\cos 2\beta - \cos 2\alpha}{2\sin^2 \gamma}$$

$$\frac{2\sin(\beta + \alpha)\sin(\alpha - \beta)}{2\sin^2 \gamma} = \frac{\sin(a - b)}{\sin \gamma} = \frac{\sin(\alpha - \beta)}{\sin(\alpha + \beta)}$$



$$\text{Prove } \alpha = 2x \quad \angle BDA = \alpha$$

$$(y + 1)^2 = 3^2 + 4^2 \quad \tan \alpha = \frac{4}{3}$$

$$(y + 1)^2 = 25 \Rightarrow y + 1 = 5 \Rightarrow y = 4$$

We want to prove $\alpha = 2x$

$$\tan x = \frac{2}{4} = \frac{1}{2}$$

$$\tan 2x = \frac{2 \cdot \frac{1}{2}}{1 - \frac{1}{4}} = \frac{1}{\frac{3}{4}} = \frac{4}{3} = \tan \alpha$$

$$2x = \alpha$$