

Function y'

$$y = x + \frac{1}{x}$$

we know that $x \neq 0$

$$x < 0 \Rightarrow y < 0$$

$$x > 0 \Rightarrow y > 0$$

There is no meeting points with $y = x$

We check $x + \frac{1}{x} = a$

$$x^2 - ax + 1 = 0$$

$$\Delta = a^2 - 4 \geq 0$$

$$a \leq -2 \text{ or } a \geq 2 \Rightarrow y \geq 2 \text{ or } y \leq -2$$

$$y = x + \frac{1}{x}$$

$$y' = 1 - \frac{1}{x^2} = 0, \quad \text{extreme points}$$

$$1 - \frac{1}{x^2} = 0 \Rightarrow x^2 = 1, \quad x = \pm 1$$

