

Equation Trigo

We have equation with trigo

Example :

$$\sin x = 1 \quad * \quad \sin x = \sin \alpha$$

$$\sin^2 x = \frac{1}{4} \quad * \quad x = \alpha + 360k \quad (180-\alpha)+360k$$

$$\sin x = \cos x \quad *$$

$$\sin 2x = \cos 2x \quad * \quad \cos = \cos \alpha$$

$$x = \pm \alpha + 360k$$

$$\cos^4 \frac{x}{2} - \sin^4 \frac{x}{2} = 1$$

$$a^2 - b^2 = (a - b)(a + b)$$

$$\left(\cos^2 \frac{x}{2} - \sin^2 \frac{x}{2}\right) \left(\cos^2 \frac{x}{2} + \sin^2 \frac{x}{2}\right) = 1$$

$$\cos x = 1$$

$$\cos x = \cos 0$$

$$x = 0 + 360k$$

prove $\sin x < \frac{1}{2}$

$$\cos^2 x - 4\sin x + \frac{5}{4} > 0$$

$$(1 - \sin^2 x) - 4\sin x + \frac{5}{4} > 0$$

$$\sin x = a$$

$$1 - a^2 - 4a + \frac{5}{4} > 0$$

$$a^2 + 4a - 2\frac{1}{4} < 0$$

$$a = \frac{-4 \pm \sqrt{16+9}}{2} \quad \begin{matrix} \swarrow \frac{1}{2} \\ \searrow -\frac{9}{2} = -4\frac{1}{2} \end{matrix}$$

$$-4\frac{1}{2} < a < \frac{1}{2}$$

$$-1 \leq \sin x < \frac{1}{2}$$