

Max – Min

$$y = \frac{x-4}{(x+1)^2} \quad x \neq -1$$

$$y' = \frac{(x+1)^2 - 2(x+1)(x-4)}{(x+1)^4}, \quad y' = 0$$

$$y' = \frac{(x+1)[x+1-2(x-4)]}{(x+1)^4} = \frac{(x+1)(-x+9)}{(x+1)^4} = 0$$

$$x = 9$$

$$y = \frac{5}{100} = \frac{1}{20}$$

x	x = -1	X = 9
y'	-----	+++++0 -----
y	↘	↗ Max ↘

Max (9, ?)

$$y = \frac{x-4}{(x+1)^2}$$

Max (9, $\frac{1}{20}$)

when $x > 4$, $y > 0$

When $x < 4$, $y < 0$

Prove that

$$\frac{x-4}{(x+1)^2} \leq \frac{1}{20}$$

$$20(x-4) \leq (x+1)^2$$

$$(x+1)^2 \geq 20x - 80$$

$$x^2 + 2x + 1 \geq 20x - 80$$

$$x^2 - 18x + 81 \geq 0, \quad a^2 - 2ab + b^2 = (a-b)^2$$

$$(x-9)^2 \geq 0$$

(9, $\frac{1}{20}$) Max

